1.1 Basic Physical Units

1.1.1 **SI Units**

Table 1.1 Fundamental and supplementary SI units.

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Prefix	Symbol	Factor	Prefix	Symbol	Factor	
yotta	Y	10^{24}	deci	d	10^{-1}	
zetta	Z.	10^{21}	centi	C	10^{-2}	
exa	E	10^{18}	milli	m	10^{-3}	
peta	Р	10^{15}	micro	μ	10^{-6}	
tera	т	10^{12}	nano	n	10^{-9}	
giga	G	10 ⁹	pico	р	10^{-12}	
mega	M	10^{6}	femto	f	10^{-15}	
kilo	k	10^3	atto	a	10^{-18}	
hecto	h	10 ²	zepto	7.	10^{-21}	
deca	da	10 ¹	yocto	V	10^{-24}	

Table 1.2 Standard prefixes for SI units.

1.1.2 **cgs-Gaussian Units**

For a useful overview of non-SI units, see [1].

Table 1.3 Comparison of SI and cgs units.

1.2

Maxwell's Electromagnetic Equations

Table 1.4 Maxwell's equations.

Table 1.4 (continued)

	SΙ	cgs-Gaussian	
$\nabla \cdot \mathbf{D}$	$= \rho_c$	$=4\pi\rho_c$	Poisson equation
$\nabla \cdot \mathbf{B}$	$= 0$	$= 0$	
D	$=\epsilon_{r}\epsilon_{0}E$	$= \epsilon_r E$	
B	$=\mu_{\rm r}\mu_0H$	$= \mu_r H$	

Boundary conditions The boundary conditions at an interface for Maxwell's electromagnetic equations are that the tangential component of *E*, and the normal component of *B*, must each be continuous, where normal means parallel to the local normal vector to the interface, and tangential means in the plane perpendicular to the local normal.

1.3 Special Relativity

Assume standard inertial frames *S* and *S'*, with respective Cartesian coordinates (x, y, z) , (x', y', z') aligned such that the origins *O*, *O'* are coincident at time $t = t' - 0$, with *S'* moving with velocity u with respect to *S*. Subscript \parallel will denote *t* $t' = 0$, with *S*^{*'*} moving with velocity *v* with respect to *S*. Subscript || will denote
the direction of this mutual motion, and subscript || denotes the orthogonal plane the direction of this mutual motion, and subscript \perp denotes the orthogonal plane. The Lorentz transformations of various physically significant quantities are given in the following table [2]:

Table 1.5 Lorentz transformations.

1.4

Physical Constants

The values of the constants quoted here are the 2006 CODATA recommended values [3].

Quantity	Symbol	Value	Units
Speed of light in vacuum	\mathcal{C}	299 792 458	$\mathrm{m}\,\mathrm{s}^{-1}$
Magnetic constant	μ_0	$4\pi \times 10^{-7}$	$\rm{H\,m^{-1}}$
Electric constant	ϵ_0	$8.854187817 \times 10^{-12}$	$F m^{-1}$
Vacuum impedance	Z_0	376.730313461	Ω
Gravitational constant	$\mathcal{C}_{\mathcal{I}}$	$6.67428(67) \times 10^{-11}$	m^3 kg ⁻¹ s ⁻²
Planck constant	h	$6.62606896(33) \times 10^{-34}$	J s
Planck mass	$m_{\mathcal{P}}$	$2.17644(11) \times 10^{-8}$	kg
Planck length	$l_{\mathcal{P}}$	$1.616252(81) \times 10^{-35}$	m
Planck time	$t_{\mathcal{P}}$	5.391 24(27) $\times 10^{-44}$	S
Avogadro constant	$N_{\rm A}$	6.022 141 79(30) \times 10 ²³	$mol-1$
Bohr magneton	μ _R	$927.400915(23) \times 10^{-26}$	$J T^{-1}$
Bohr radius	a ₀	$0.52917720859(36) \times 10^{-10}$	m
Boltzmann constant	$k_{\rm B}$	$1.3806504(24) \times 10^{-23}$	$J K^{-1}$
Elementary charge	e	1.602 176 487(40) \times 10 ⁻¹⁹	C
Fine structure constant	α	7.297 352 537 6(50) \times 10 ⁻³	
	α^{-1}	137.035 999 679(94)	
Molar gas constant	R	8.314 472 (15)	$J \text{ mol}^{-1} K^{-1}$
Nuclear magneton	μ_N	$5.05078324(13) \times 10^{-27}$	J^{-1}
Rydberg constant	R_{∞}	10 973 731.568 527(73)	m^{-1}
Stefan-Boltzmann constant	σ	$5.670400(40) \times 10^{-8}$	$W m^{-2} K^{-4}$
Thomson cross section	$\sigma_{\rm e}$	$0.6652458558(27) \times 10^{-28}$	m ²
Wien constant	b	$2.8977685(51) \times 10^{-3}$	m K
α Particle:			
Mass	m_a	$6.64465620(33) \times 10^{-27}$	kg
– electron mass ratio	m_α/m_e	7.294 299 536 5(31) \times 10 ³	
- proton mass ratio	m_α/m_p	3.972 599 689 51(41)	
Deuteron:			
Mass	m_d	3.343 583 20(17) \times 10 ⁻²⁷	kg
– electron mass ratio	m_d/m_e	$3.6704829654(16) \times 10^3$	
- proton mass ratio	m_d/m_p	1.999 007 501 08(22)	
magnetic moment	μ _d	$4.33073465(11) \times 10^{-27}$	$J T^{-1}$

Table 1.6 Values of physical constants.

 \mathbf{I}

Table 1.6 (continued)

1.5 Dimensional Analysis

Table 1.7 Dimensions of common variables.

1.6

Ionization Energies of Gas-Phase Atoms and Molecules

The energies of first ionization *E*ⁱ for certain gas-phase molecules are given here, selected from [4]

Table 1.8 Ionization energies of gas-phase atoms and molecules

Substance	Formula	E_i/eV		
Acetylene	C ₂ H ₂	11.400		
Ammonia	NH ₃	10.070		
Argon	Ar	15.75962		

 \mathbf{I}

Table 1.8 (continued)

1.7

Electron Affinities of Selected Atoms and Molecules

The electron affinity E_A is defined to be the energy difference between the ground state of the neutral, and the lowest energy state of the corresponding negative ion. If $E_A > 0$, then the negative ion is stable; if $E_A < 0$, the negative ion is unstable. Selected data is presented below, drawn from [4, 5]

Table 1.9 (continued)

1.8 Atomic and Molecular Notation

1.8.1 **Atomic Electron Configurations**

The electronic configuration in atoms is characterized by four quantum numbers (n, l, m_l, m_s) that define the distribution of electrons across the available atomic levels and orbitals, with no two electrons allowed to share the same four quantum numbers (the Pauli Principle). The classification is arranged in descending significance in terms of energy contribution.

1.8.1.1 **Principal Quantum Number,** *n*

Levels are denoted by the principal quantum number, *n*, which can take integer values $n = 1, 2, 3...$ and which is the main determinant of electron energy. Atomic states with different *n* have significantly different energies. Historical notation for the principal quantum number is $K(n = 1)$, $L(n = 2)$, $M(n = 3)$ and so on, alphabetically (a notation usually used in X-ray spectra). For each value of *n*, there are *n* subshells, identified by the angular momentum (or azimuthal) quantum number *l*.

1.8.1.2 **Azimuthal Quantum Number,** *l*

Each subshell or sublevel (sometimes referred to as orbital) is denoted by the angular momentum (or azimuthal) quantum number *l*, which can take take integer values from 0 to $n-1$. These refer to the quantization of the orbital angular momentum of an electron in the subshell, and leads to the overall shape of the orbital (see Figure 1.1). A conventional notation for the first four *l*-values is $s(l = 0)$, $p(l = 1)$, $d(l = 2)$ and $f(l = 3)$; the notation continues alphabetically with $g(l = 5)$ and so on. Each subshell can contain a maximum of $2(2l + 1)$ electrons, which can occupy states characterized by m_l and m_s .

Figure 1.1 The angular dependence of the *s*, *p* and *d* orbitals, showing symmetry about the principal (horizontal) axis.

1.8.1.3 **Magnetic Quantum Number,** *ml*

Given that an electron is in subshell *l*, its angular momentum component along the principal axis (the main symmetry axis for the wavefunctions) is further quantized by the magnetic quantum number m_l , which can take integer values in the range $(l-l, -l+1, \ldots, 0, \ldots, l-1, l)$, yielding $2l + 1$ states in total.

1.8.1.4 **Spin Quantum Number,** *m***s**

Finally, there are two spin states for each electron in any n, l, m_l state: spin-up and spin-down, corresponding to $m_s = \pm \frac{1}{2}$.

As a consequence of the distribution of electrons across the possible angular momentum, magnetic and spin quantum states, the total number of electrons in each of the principal quantum levels is $2n^2$, as can be seen from Table 1.10. In the standard notation for the configuration of electrons in an atom, each shell and subshell is given as a character string, with the number of electrons in each subshell stated as a superscript on the *l* value: for example, the configuration of electrons in He can be stated as $1s^2$; for Carbon atoms, $1s^2 2s^2 2p^2$, and so on. The ground-state configuration of selected atoms is given in Table 1.11.

Table 1.10 Atomic notation: under each principal quantum number, the subshells are denoted, along with the number of electrons per subshell.

							$n = 1$ (K) $n = 2$ (L) $n = 3$ (M) $n = 4$ (N) $n = 5$ (O)			
$l=0$	1s	2	2s	2	3s	2	4s	2	5s	
$l=1$			2p	6	3p	6	4p	6	5p	6
$l=2$					3d	10	4d	10	5d	10
$l = 3$							4f	14	5f	14
$l = 4$									5g	18
Total		\mathcal{L}		8		18		32		50

Table 1.12 Selected significant spectral lines of atomic and singly ionized elements, as observed in air, and chosen for the greatest relative intensity; * denotes Fraunhofer lines.

Atomic spectra arise when electrons make the transition from one set of (*n*, *l*, m_l , m_s) to another, losing energy by emission of photons (or gaining energy by absorption). Examples of important spectra are given in Table 1.12.

1.8.1.5 **Multielectron Atoms**

For atoms with several electrons [6], there is strong electrostatic coupling between the orbital angular momentum and the spins across the populated states, leading to additional energy structure in the electronic configuration.

The total resultant orbital angular momentum vector arising from the *li* of the electrons in the atom is a quantum vector denoted as *L*. The underlying quantization comes from the interaction of electrons with different values of *n* and *l*, and is expressed in the quantum-mechanical vector addition of the associated vector angular momenta l_i to produce a resultant total orbital angular momentum L , the possible quantized values of which are given by m_l . In a similar way, the resultant of the quantum spins over the $m_{s,i}$ is designated by *S*. These resultants, *L* and *S*, can be added to produce a total resultant angular momentum *J* of the electrons in the atom, which is also quantized. The magnitude of the quantized resultant of *L* and *S* can only take the values $L + S$, $L + S - 1$, ..., $|L - S|$, denoted by *J* (this is a general rule for all quantum vectors).

The states $L = 0, 1, 2, 3, \ldots$ are labeled *S*, *P*, *D*, *F* by analogy with the *l* values, with the series continuing alphabetically beyond $L = 4$. (Note that electrons in closed shells do not contribute to this coupling.) An additional fine-structure arises in each *L*-state, when magnetic interactions (from the intrinsic dipole moments of the electrons) are taken into account. States that are formed in this way are deemed to have multiplicity $2S + 1$ and form multiplet states, designated by the *L* value letter, with left superscript showing the multiplicity of the state, and right subscript giving the corresponding *J* value.

For example, if an atom has an *f*-electron ($l = 3$) and a *d*-electron ($l = 2$), then the possible values of *L* are $3 + 2 = 5$, 4, 3, 2 and $|3 - 2| = 1$. In a similar way, the possible values of *S* are 0 and 1. Hence, the multiplet states are *P*, *D*, *F*, *G* and *H*, each of which can have $S = 0$ (with multiplicity 1, and therefore are singlet states) or $S = 1$ (with multiplicity 3, and so are triplet states). The singlet states are then ¹ $P_1(L = 1, S = 0, I = 1)$, ¹ $D_2(L = 2, S = 0, I = 2)$ and so on, with the triplet states as ${}^{3}P_{2}(L = 1, S = 1, I = 2), {}^{3}D_{3}(L = 2, S = 1, I = 3)$ and so on.

1.8.1.6 **Selection Rules for Transitions**

For electric dipole transitions, the following rules apply:

- 1. Δ*n* unrestricted
- 2. $\Delta l = \pm 1$
- 3. $\Delta L = 0, \pm 1$ except $0 \leftrightarrow 0$
- 4. $\Delta S = 0$
- 5. $\Delta I = 0, \pm 1$ except $0 \leftrightarrow 0$

1.8.1.7 **Emission and Absorption**

The spectral emission coefficient $\varepsilon(\nu)$ due to a spontaneous electronic transition from an upper state *u* to a lower state *l* in an atom resulting in the emission of a photon of frequency nu_0 is given by

$$
\varepsilon = \frac{n_{\rm u} A_{\rm ul}}{4\pi} h \nu \Phi (\nu - \nu_0) \tag{1.1}
$$

where *n*^u is the population of the upper level, *A*ul is the Einstein coefficient for spontaneous emission, nu_0 is the line center defined by $hnu_0 = E_u - E_l$, where $E_{\mu l}$ denotes the energy level of the upper and lower atomic states, and Φ is the lineshape function, which describes natural and instrumental line-broadening mechanisms.

In the case of electric dipole transitions, A_{ul} is defined to be

$$
A_{\rm ul} = \frac{64\pi^4 \nu^3}{3\epsilon_0 h c^3} \mu_{\rm ul}^2 \tag{1.2}
$$

where μ_{ul} is the transition dipole moment.

1.8.2

Molecular Electron Configurations

The configurations of electrons in molecules is more complicated than the single atom case because the nuclear motion of the constituent species influences the electron energy levels, along with the persistent internuclear electric field that bonds the molecule together [7, 8].

The ground electronic state of a molecule is designated by *X*, with excited states of the same multiplicity (i.e., spin quantum number in Section 1.8.2.3) as the

ground state denoted by *A*, *B*, *C*, . . . in ascending order of energy; if excited states have a different multiplicity from the ground state, then these states are labeled with lower-case letters *a*, *b*, *c*, ... The details of the electronic configurations in such states is given in the following paragraphs, which apply mainly to diatomic molecules.

1.8.2.1 **Born–Oppenheimer Approximation**

The Born–Oppenheimer approximation separates out the nuclear motion (vibration and rotation) from the electron behavior, under the assumption that the electrons will move much faster than the heavier nuclei. This assumption means that the electronic transition energies E_{el} (a few eV) are taken to be much larger than the vibrational energies *E*vib (around 0.1 eV), which in turn are much larger than the rotational energies E_{rot} (a few meV):

$$
E_{\rm el} \gg E_{\rm vib} \gg E_{\rm rot} \tag{1.3}
$$

1.8.2.2 *Λ* **Quantum Number**

Assuming that the Born–Oppenheimer approximation (Section 1.8.2.1) holds, the electronic configuration is characterized in a similar way to atomic electrons in that the quantum numbers $(n_1, l_1, n_2, l_2, \ldots)$ produce different quantized energy levels associated with the quantum vectors *L*, *S* and *J*; however, the quantizing axis is the internuclear one, and the resultant orbital angular momentum along this axis is designated Λ , with states $\Lambda = 0, 1, 2, \ldots$ given the notation Σ , Π , Δ and so on, analogous with the *S*, *P*, *D* atomic *L* states.

1.8.2.3 **Spin Quantum Number**

Coupling of electron spins to the internuclear axis is weak, and so the resultant (total) *S* is much the same as for atoms; however, *S*, the axial component of *S* (and not to be confused with the Greek letter indicating the Λ value), plays a key role in diatomic molecules, coupling to Λ to form a resultant Ω , the total electronic angular momentum along the internuclear axis. $\Omega = |A + S|$, in a similar way to *J* for atoms. Hence, Ω can take the values $A + S$, $A + S - 1$, ..., $|A - S|$, and such states are deemed to have a (spin) multiplicity $2S + 1$ (known as spinsplitting). Each such state can be subdivided into two Λ -substates, giving a total degeneracy of $(2S + 1)(2 - \delta_{0,1})$ where $\delta_{i,j} = 1$ if $i = j$ and 0 otherwise, is the Kronecker delta.

1.8.2.4 **Molecular Term Notation**

The molecular notation then is as follows: the Λ state is written with a left superscript denoting the associated multiplicity of the of Σ value, and a right subscript giving the maximum *Ω* value. Hence, a state with *S* = 0, *Λ* = 0 is written as ¹*Σ* (see Table 1.13); for the state with *S* = 1, *Λ* = 1 (and therefore, *Ω* = *2*) is written by ${}^{3}H_{2}$. This notation is preceded by a letter denoting the multiplicity of the state: *X* is ground state, and multiplicities are given by *A*, *B*, *C* if they have the same multiplicity as the ground state, otherwise lower case letters are used.

Term	State		g
1Σ	singlet sigma	$S = 0, A = 0$	1
2π	doublet pi	$S = 1/2, \Lambda = 1$	$\overline{4}$
3Σ	triplet sigma	$S = 1, A = 0$	3
3π	triplet pi	$S = 1, A = 1$	6
2Λ	doublet delta	$S = 1/2, \Lambda = 3$	4

Table 1.13 Molecular electronic state notation, showing the associated quantum numbers and electron degeneracy *g*.

1.8.2.5 **Symmetry**

The symmetry of the electron orbitals is a further complication: for a homonuclear molecule, the electron density must be symmetric with respect to the midpoint between the nuclei (that is, the center of mass), but the wavefunction of the electron can be even or odd parity, denoted *g* or *u*, respectively (from the German *gerade* and *ungerade*). For Σ states, symmetry of the wavefunction with respect to a mirror reflection through a plane containing the internuclear axis is denoted by a right superscript $+$ if symmetric; $-$ if not.

1.8.2.6 **Selection Rules for Transitions**

Electric dipole transitions between electronic levels in diatomic molecules obey the following selection rules:

- 1. $\Delta \Sigma = 0$ (no change in total electron spin)
- 2. $\Delta A = 0, \pm 1$
3. $u \leftrightarrow g$
- 3. $u \leftrightarrow g$
4. ∇^+
- 4. $\Sigma^+ \leftrightarrow \Sigma^+$ or $\Sigma^- \leftrightarrow \Sigma^-$

The spectra of molecules is considerably more complex than that of atoms because of the more extensive range of possible transitions. Molecular spectra consist of bands, which are very tightly grouped series of emission (or absorption) lines within an amplitude envelope that may extend only for a few nanometers. The spacing of the lines within the band head is controlled by electron transitions between the molecule's rotational states. The envelopes are not symmetric: the conspicuous sharp edge is termed the band head, with the envelope fading smoothly in amplitude towards increasing wavelength (termed 'degraded to red') or decreasing wavelength ('degraded to violet').

Certain molecules exhibit very extensive band systems that span wide spectral ranges with little variation in band intensity or structure, such as H_2 (more than 100 strong bands between 406 and 835 nm), Cl_2 (mixture of continuum and band emission in 480–600 nm, strong continuous absorption in 250–400 nm), CO (198– 860 nm, including third positive, Asundi, triplet, Cameron, 3A, Knauss & Kaplan bands, in addition to those in Table 1.14).

Table 1.14 Selected significant molecular spectral bands, as observed in air, and chosen for greatest relative intensity; § denotes extensive number of bands of similar intensity in the indicated wavelength range, with more

prominent heads identified in final column; r, v denotes degraded to red, violet; * denotes forbidden line. Data taken from [9], with additional information on ozone from [10].

^a Seen in emission in comet tails, but in absorption in solar spectrum.

b 314.34 is only v, and is most intense.

^c Seen in absorption in stellar spectra.

^d Can be detected in sunspots.

1.9 Characteristic Parameters for Typical Plasmas

1.9.1 **Laboratory Plasma Reactors**

There is a wide variety of vessel and electrode geometry in laboratory devices; the following list is indicative, but not exhaustive. Table 1.16 gives typical operating parameters for various plasma devices.

1.9.1.1 **Corona Discharge**

Also known as 'point-to-plane' discharge [11, 12], the ionizing electric field is produced by a marked asymmetry in the electrodes. The standard configuration, shown in Figure 1.2, is a sharply pointed electrode paired with a planar electrode, with the former producing a localized high electric field sufficient to ionize the neutral gas, and strike a plasma; a similar effect can be produced by electrodes in the form a wire inside a hollow cylinder. The ionization region is generally confined to a small area close to the high-field electrode, producing a drift region (between the ionization region and the flat electrode) in which charged particles (mainly electrons) react with neutrals and induce electron-moderated chemical reactions, including radical production. If the electric field is very high, plasma streamers can extend the ionizing region to encompass the second electrode. It is suitable for use over a wide range of pressures (including atmospheric), with applications that include ozone production, surface modification and combustion promotion.

1.9.1.2 **Dielectric Barrier Discharge**

Also known as silent discharges, dielectric barrier discharges (DBD) [13] generally consist of a pair of AC-powered plane electrodes with at least one covered in a dielectric layer (Figure 1.3). The neutral gas breaks down in the usual manner, forming streamers. However, when the streamers bridge the gap between the elec-

Figure 1.2 Typical configuration of a point-to-plane corona discharge, showing a plasma ionization region close to the high field at the point electrode, and the region of ion drift impinging on the flat electrode plate.

Figure 1.3 Typical configuration of a dielectric barrier discharge (DBD), showing the powered electrodes and the dielectric layers; though two dielectric layers are shown, it is only necessary to have one dielectric layer present in the discharge gap.

trodes, the dielectric layer allows free charge to accumulate which significantly affects the ongoing development of the discharge, including self-quenching. In particular, charge accumulated from one half-cycle of AC power is available to enhance the field in the subsequent half-cycle.

1.9.1.3 **GEC Reference Cell**

A standard parallel plate, capacitively-coupled rf plasma reactor designed for researching plasma discharge phenomena of direct relevance to the plasma technology sectors [14]. By designing a standard reactor for general use in different plasma conditions, the effects of reactor geometry could be minimized. Figure 1.4 shows a simplified schematic of a typical arrangement; in fact, either electrode can be powered independently, and the electrode spacing can be adjusted. Not shown on the schematic are the 8 diagnostic ports in the midplane. The showerhead electrode has 169 equally spaced holes placed in concentric circles for smooth gas feeding; the reactor is designed to work at a base pressure close to 10^{-5} Pa. Gas flow rates in the range 2–25 sccm (standard cubic centimeters per second) can be accommodated. At 10 sccm, the reactor pressure is generally not below 8 Pa.

1.9.1.4 **Hollow Cathode Discharge**

Hollow cathode devices (HCDs) [15–17] have the cathode in the form of a cup or cylinder, closed at one end, with the anode near the open end of the cathode (Figure 1.5). This arrangement allows the HCD to operate in the transition between the glow-discharge and a low-pressure arc discharge, supporting high current density negative glow (electron current) enclosed within the cathode structure. Because of their greater efficiency compared to a conventional plane-parallel electrode arrangement, HCD are used in spectral analyses of gas samples, and are valuable as photon sources (lamps). Microhollow cathode discharges (MHCDs) are similar in concept to HCD but are very much smaller, having scale lengths in the 10 s of mm. MHCD are often referred to as microdischarges, though the latter term additionally refers to devices which are similar in topology to HCD, but operate at atmospheric pressures and using AC power.

Figure 1.4 Simplified schematic of a Gaseous Electronics Conference (GEC) Reference Cell, showing the showerhead upper electrode and powered lower.

Figure 1.5 Simplified schematic of a typical hollow cathode discharge arrangement.

1.9.1.5 **Tokamak**

The primary device for magnetic confinement fusion, the tokamak holds deuterium–tritium plasma in a toroidal chamber, shown schematically in Figure 1.6. The strong toroidal magnetic field (shown in bold arrow) is imposed by external field coils (not shown), and combines with the poloidal self-field of the plasma; the resultant helical magnetic field structure inhibits the plasma from touching the vacuum vessel. The toroidal (or major) radius *R* and poloidal (or minor) radius *r* are key

Figure 1.6 Schematic of a tokamak reactor, showing the major *R* and minor *r* radii for a circular cross-section vessel.

Table 1.15 Selected critical data for various tokamaks. § denotes spherical tokamak.

^a Superconducting coils.

Table 1.16 The operating parameters for rf parallel plate plasma etching, and high-density plasma reactor [18].

^a Standard cubic centimeters per second.

parameters in determining the reactor geometry. The main fusion reaction is as follows:

$$
{}_{1}^{2}D + {}_{1}^{3}T \rightarrow {}_{2}^{4}He + {}_{0}^{1}n
$$
 (1.4)

where the neutron has 14.1 MeV energy. Deuterium is a naturally occurring isotope of hydrogen; tritium has a short half-life of 12.3 years, and so has negligible natural abundance. Instead, it can be bred from lithium via the following reactions:

$$
{}_{0}^{1}n + {}_{3}^{6}Li \rightarrow {}_{1}^{3}T + {}_{2}^{4}He
$$
 (1.5)

$$
{}_{0}^{1}n + {}_{3}^{7}Li \rightarrow {}_{1}^{3}T + {}_{2}^{4}He + {}_{0}^{1}n
$$
 (1.6)

Table 1.15 gives characteristic data for a range of tokamaks. Spherical tokamaks are devices in which the major radius is reduced to a minimum, as they are essentially spheres with a central column dividing the chamber, making them formally toroidal in topological form.

1.9.2 **Terrestrial and Solar Plasmas**

The data in this section characterizes the distribution of neutral and ionized species throughout the atmospheres of the earth and the sun.

Table 1.17 Ionospheric parameters [19].

Figure 1.7 Model atmosphere MSIS E 90 from the Virtual Ionosphere, Thermosphere, Mesosphere Observatory (VITMO). The curves show the Nitrogen molecule number density (lefthand axis) and temperature (right-hand axis) as a function of height above sea level.

Figure 1.8 Model atmosphere as for Figure 1.7. The curves show the relative abundance by number of various chemical species (left-hand axis) and temperature (right-hand axis) as a function of height above sea level.

Figure 1.9 Model Ionosphere based on International Reference Ionosphere IRI 2007, for which the heights of the various regions are as follows: D: 88 km; E: 110 km; and F₂: 350 km.

Plots shown are electron density (left-hand vertical axis), electron and ion temperatures (right-hand vertical axis) as functions of height.

Figure 1.10 Model Ionosphere based on International Reference Ionosphere IRI 2007, for which D region height is 88 km, E 110 km, F₂ 350 km. Plots shown are electron density (left-hand vertical axis), and relative ion abundance (right-hand vertical axis) as functions of height.